Adjusting for Unmeasured Spatial Confounding with Distance Adjusted Propensity Scores

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# Air Quality Regulations

Regulations

- Clean Air Interstate Rule (CAIR)
- Cross-State Air Pollution Rule (CSAPR)
- 1990 Clear Air Act
- Acid Rain Program
- Power plants followed various compliance strategies
- Comparative effectiveness of NO<sub>x</sub> emission control technologies on ambient ozone levels

#### $NO_x$ : Nitric oxide and nitrogen dioxides

# Motivation

■ Ozone is a secondary pollutant (Allen, 2002)

- Created from chemical reactions in the atmosphere
- Sunlight, Higher temperature
- Selective Catalytic Reduction (SCR) and Selective Non-Catalytic Reduction (SNCR) are the most effective in reducing  $NO_x$

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- Reductions in NO<sub>x</sub> emissions → reduction in ozone concentrations
- Effect of SCR/SNCR on ambient ozone

# Data

- Coal and natural gas power plants during June-August 2004
- A = 1 if at least half of facility heat input is used by units with installed SCR/SNCR technologies, A = 0 otherwise
- 152 treated facilities, 321 controls
- Y: NO<sub>x</sub> emissions /  $4^{th}$  maximum ambient ozone concentration



## For unit i

- Treatment  $A_i \in \{0, 1\}$
- Potential outcomes  $Y_i(1), Y_i(0)$  (SUTVA)
- Covariates  $C_i = (C_{i1}, C_{i2}, \dots, C_{ip})$

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- $P(A = 1 | \mathbf{C}) \in (0, 1)$
- $\bullet \ Y(1), Y(0) \amalg A | {\bf C}$
- Propensity score matching
  - PS model  $P(A = 1 | \mathbf{C})$
  - Match treated units to controls with similar PS estimates

Unmeasured spatial confounding

• Confounders  $\mathbf{C} = (\mathbf{X}, \mathbf{U})$ 

- **X** are observed, **U** are unobserved
- If U varies spatially, can we adjust for it?

# Unmeasured spatial confounding

- Confounders  $\mathbf{C} = (\mathbf{X}, \mathbf{U})$ 
  - $\blacksquare$  X are observed, U are unobserved
- If **U** varies spatially, can we adjust for it?
- Temperature, and weather conditions may confound the relationship of  $NO_x$  control strategies and ambient ozone.
  - Temperature, barometric pressure, humidity
- Weather and atmospheric covariate information varies spatially

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# Unmeasured Spatial Confounding

- Observed variables **X**:
  - Use the propensity score to adjust for the observed confounders
  - $P(A_i = 1|X_i) = f(X_i) = \operatorname{expit} (X_i^T \beta)$
- $\blacksquare$  Unmeasured spatial confounders  ${\bf U}$ 
  - The correlation of **U** is high for small enough distances
  - If a matched pair is sufficiently close, the treated and control units will have similar values of **U**

Distance Adjusted Propensity Score Matching

 $\blacksquare$  For a treated unit i and a control unit j define

$$DAPS_{ij} = w|PS_i - PS_j| + (1 - w) * Dist_{ij}, w \in [0, 1]$$

where PS propensity score estimates, and Dist spatial proximity.

- *w* expresses our belief of the relative importance of the observed and unobserved confounders
- *Dist* is the measure the expresses our belief of similarity of *U* as a function of distance

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# Choosing w

 $DAPS_{ij} = w|PS_i - PS_j| + (1 - w) * Dist_{ij}, w \in [0, 1]$ 

- Interplay between distance of observed covariates and distance of matched pairs
- *w* can be specified using subject-matter knowledge on an unmeasured spatial confounder
- Automated procedure
  - Re-calculates DAPS and performs matching for many values of w
  - Balance of the observed covariates is assessed
  - The smallest value that acheives covariate balance is chosen

## Checking covariate balance

#### $\blacksquare$ Absolute standardized difference of means as a function of w



# Matches



## • Average distance of matched pairs

- Naïve: 1066 miles
- DAPSm: 141 miles

# Results



205 NO<sub>x</sub> tons (95% CI: 4 − 406)
−0.27 parts per billion (95% CI: −2.1 − 1.56)

# DAPSm results as a function of w



#### Estimates with 95% confidence intervals for Ozone analysis

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# Conclusions

- SCR/SNCR control technologies seem to be associated with reduced NO $_x$  emissions
- Their effect on ozone is not significant
- Unobserved confounding can lead to severe bias of estimates

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