

# Quantifying bias from dependent left truncation in survival analyses of real world data

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## Background

- In many EHR-derived databases, patients are only observed if they satisfy a certain entry criteria, such as undergoing a biomarker testing procedure
- **Left truncation (LT)** arises because we do not observe any patients who experienced a disqualifying event (such as death) before satisfying the entry criteria
- When analyzing overall survival (OS), failure to account for LT results in bias, since patients observed in the database had to at least live long enough to qualify for entry

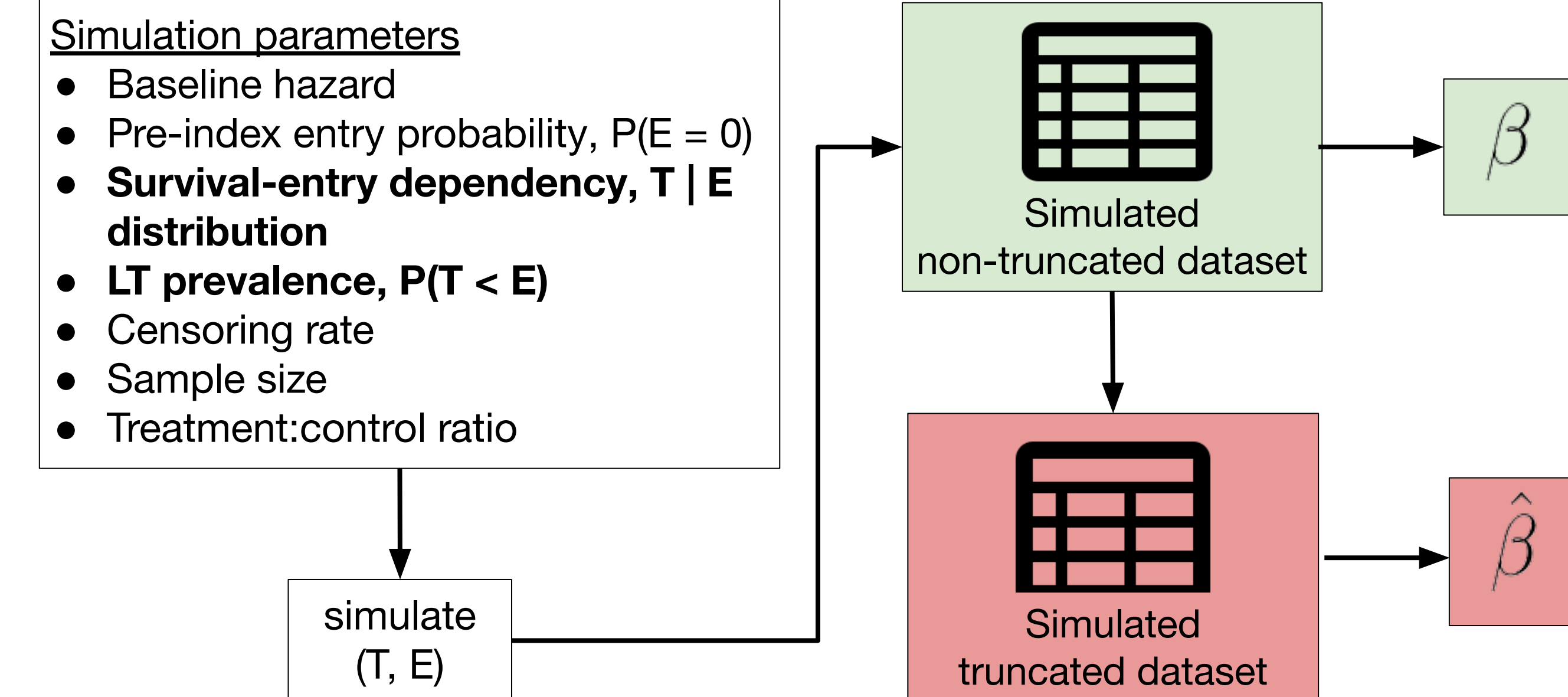
## Independent vs dependent left truncation

- Risk set adjustment for survival analyses can adjust for **independent LT**, where the survival time  $T$  and entry time  $E$  variables are independent
- This condition is testable over the observed space, but is often not satisfied (e.g. patients biomarker-tested later in their disease course may die sooner)
- Under **dependent LT**, standard methods are not guaranteed to unbiasedly estimate the marginal survival distribution
- Magnitude and direction of this bias are generally unexplored

## Contributions

- We implement simulation studies examining analyses involving survival data subject to dependent left truncation, and quantify the resulting inferential bias
- We characterize general trends in the bias, with the goal of determining when such analyses may still provide useful results
- We outline a procedure for conducting sensitivity analyses given an arbitrary dataset subject to dependent left truncation, to determine how bias in results would change when varying levels of left truncation

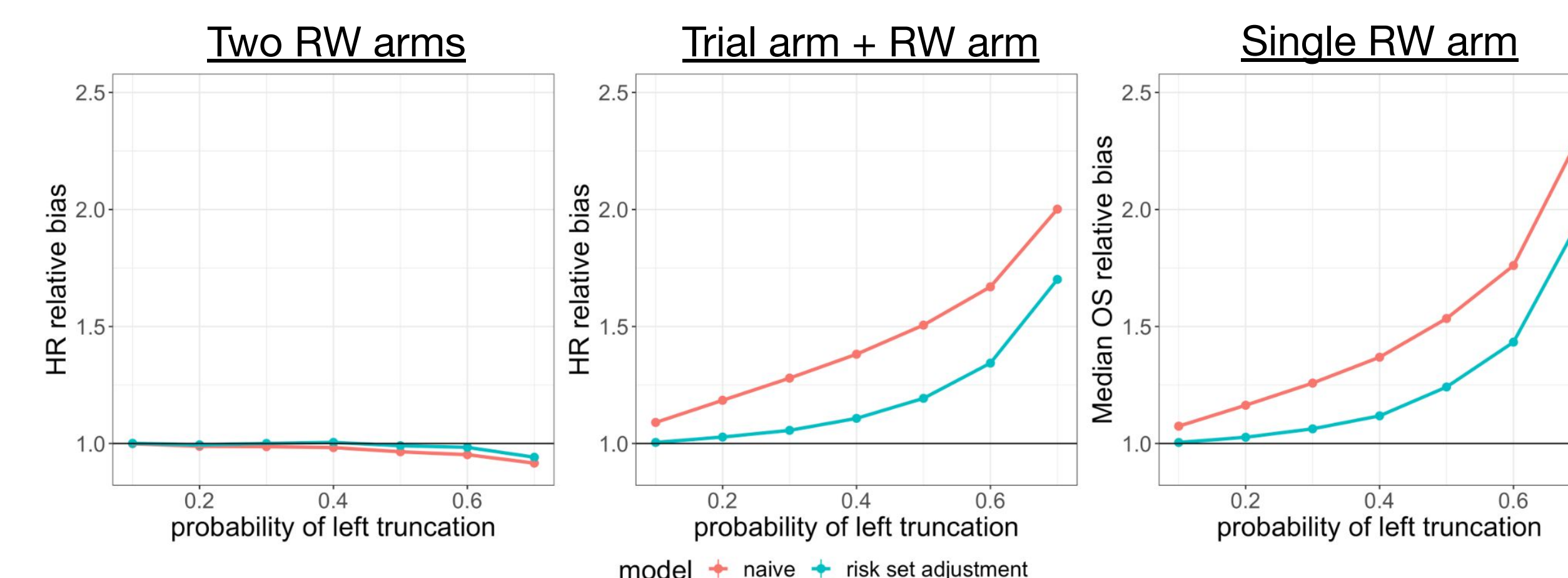
## Simulation study of dependent left truncation



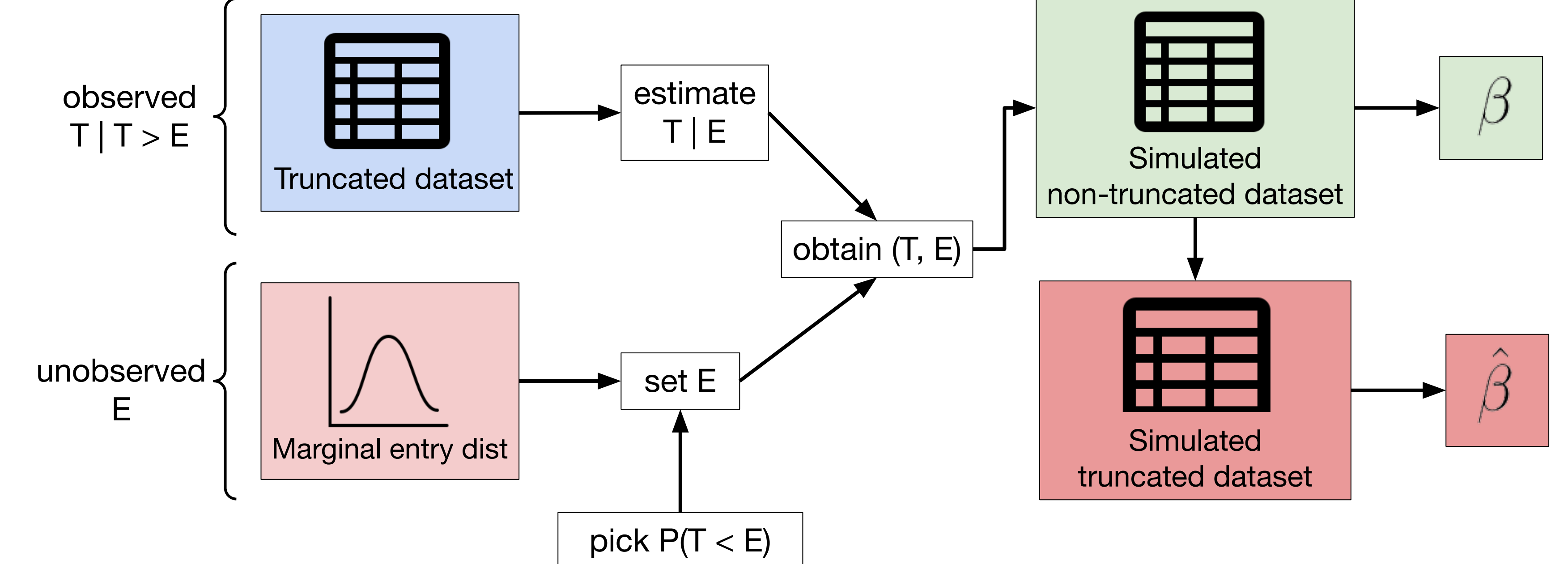
- Considered 3 designs corresponding to survival analyses performed with real world (RW) data subject to LT: (1) comparing two RW cohorts, (2) comparing a RW cohort to a non-truncated trial cohort, (3) estimating survival in a single RW cohort

## Results

- Estimator bias varies substantially between analytic settings
- Estimation of absolute quantities (e.g. median survival time) more subject to bias than that of relative quantities (e.g. hazard ratios)
- Low bias when comparing two RW arms having similar truncation
- When comparing a truncated RW arm to a non-truncated arm, the estimated hazard ratio is **biased upwards**, providing **conservative inference**
- High bias in estimating median survival in a single RW cohort



## Simulation-based sensitivity analysis



- Given an observed truncated dataset, we can estimate the conditional  $T | E$  distribution
- Then, for a particular truncation probability, we can simulate “complete” datasets, and compare truncated vs non-truncated estimates to assess sensitivity to dependent LT bias

## Conclusions

- Dependent LT can result in **high bias and invalid coverage of confidence intervals**, particularly for **absolute estimands**
- However, when comparing survival of a non-truncated trial cohort to a truncated RW cohort, the bias in the hazard ratio is guaranteed to be upwards
  - I.e. the trial treatment effect **biased towards the null**, more likely to be declared non-significant
  - In drug development, this can still provide an acceptable signal of treatment efficacy
- Our simulation settings cannot cover every possible data-generating process; we recommend that researchers apply **simulation-based sensitivity analyses** based on their own datasets
  - Most simulation parameters are estimable from truncated dataset
  - Examples and guidance for implementation can be found in manuscript

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A pre-print of this manuscript is available on medRxiv:  
<https://www.medrxiv.org/content/10.1101/2021.08.02.21261492v1>